

## 2003 AB3

3a.  $R'(45)$  is approximately equal to  $\frac{R(40) - R(50)}{40 - 50} = 1.5 \frac{\text{gal} / \text{min}}{\text{min}}$

3b. At  $t = 45$  the function  $R(t)$  is increasing fastest. After this point the slope of  $R(t)$  will decrease. This is the location where  $R''(t)$  is changing from positive concavity to negative concavity so  $R''(t)$  should be zero.

3c.

$$\int_0^{90} R(t) dt \approx 30(20) + 30(10) + 40(10) + 55(20) + 65(20)$$
$$\int_0^{90} R(t) dt \approx 3700 \text{ gal}$$

This value is less than the actual value since all rectangles are under the function or  $R(t)$  is increasing for  $0 < t < 90$  so the Left hand Riemann Sum is less than the actual area.

3d.  $\int_0^b R(t) dt =$  is the number of gallons of fuel consumed during the first  $b$  minutes of a flight.

$\frac{1}{b} \int_0^b R(t) dt =$  average rate of consumption (gallons/minute) of fuel consumed during the first  $b$  minutes of the flight.